

## Exercise 3

3. The following data are available for a linear-reservoir system:

$B_o=1.25$  bbl/STB ,  $B_w=1.02$  bbl/STB ,  $h = 20$  ft ,  $A = 26400$  ft<sup>2</sup> , Porosity = 25%

Injection rate  $i_w = 900$  bbl/day, distance between producer and injector  $L=600$  ft,

$u_o=2.0$  cp,  $u_w =1.0$  cp, Dip angle =  $0^\circ$  ,  $S_{wi}=20\%$  ,  $S_{or} = 20\%$

Seek for:

- (1) Plot the water saturation profile after 60, 120, and 240 days.
- (2) Calculate time to breakthrough?
- (3) Calculate cumulative water injected at breakthrough?
- (4) Calculate total pore volumes of water injected at breakthrough?

$S_w$	$k_{ro}/k_{rw}$
0.25	30.23
0.30	17.00
0.35	9.56
0.40	5.38
0.45	3.02
0.50	1.70
0.55	0.96
0.60	0.54
0.65	0.30
0.70	0.17
0.75	0.10

$$\frac{df_w}{dS_w} = \frac{\left(\frac{\mu_w}{\mu_o}\right) b a e^{-bS_w}}{\left[1 + \left(\frac{\mu_w}{\mu_o}\right) a e^{-bS_w}\right]^2} = \frac{\left(\frac{\mu_w}{\mu_o}\right) b \left(\frac{K_{ro}}{K_{rw}}\right)}{\left[1 + \left(\frac{\mu_w}{\mu_o}\right) \left(\frac{K_{ro}}{K_{rw}}\right)\right]^2}$$

**Note:**

The frontal advance equation:

$$(x)_{S_w} = \frac{q_i t}{\phi A} \left( \frac{\partial f_w}{\partial S_w} \right)_{S_w}$$

**In field units**, the above equation can be expressed as:

$$(x)_{S_w} = \left( \frac{5.615 i_w t}{\phi A} \right) \left( \frac{df_w}{dS_w} \right)_{S_w}$$